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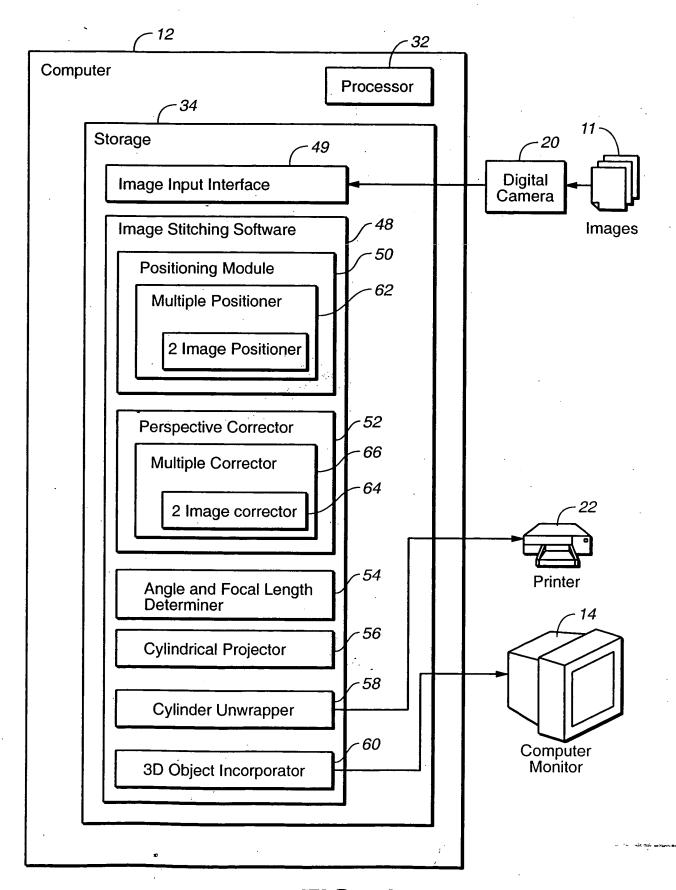
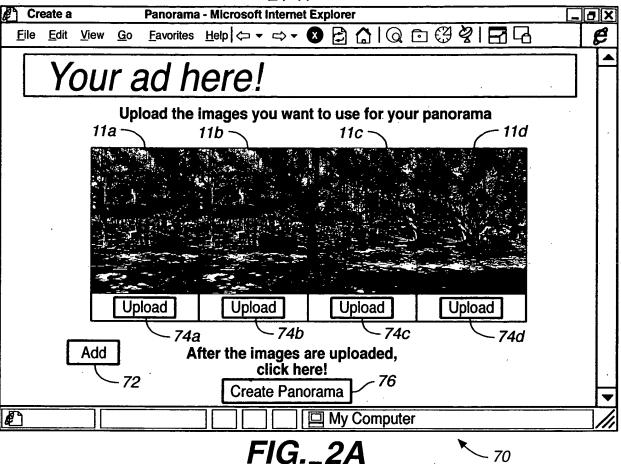
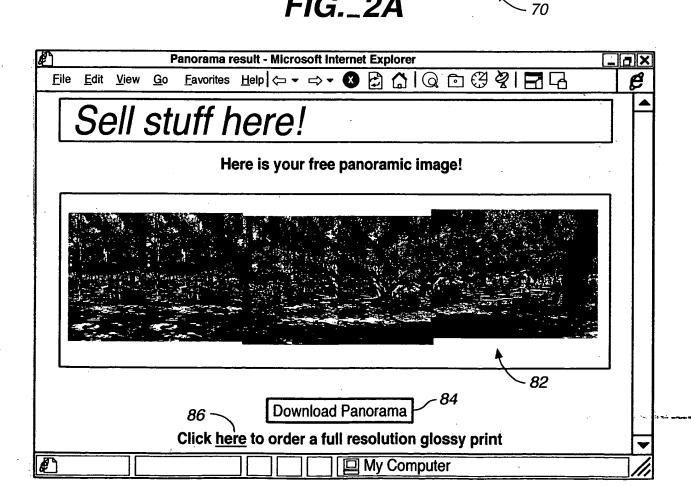


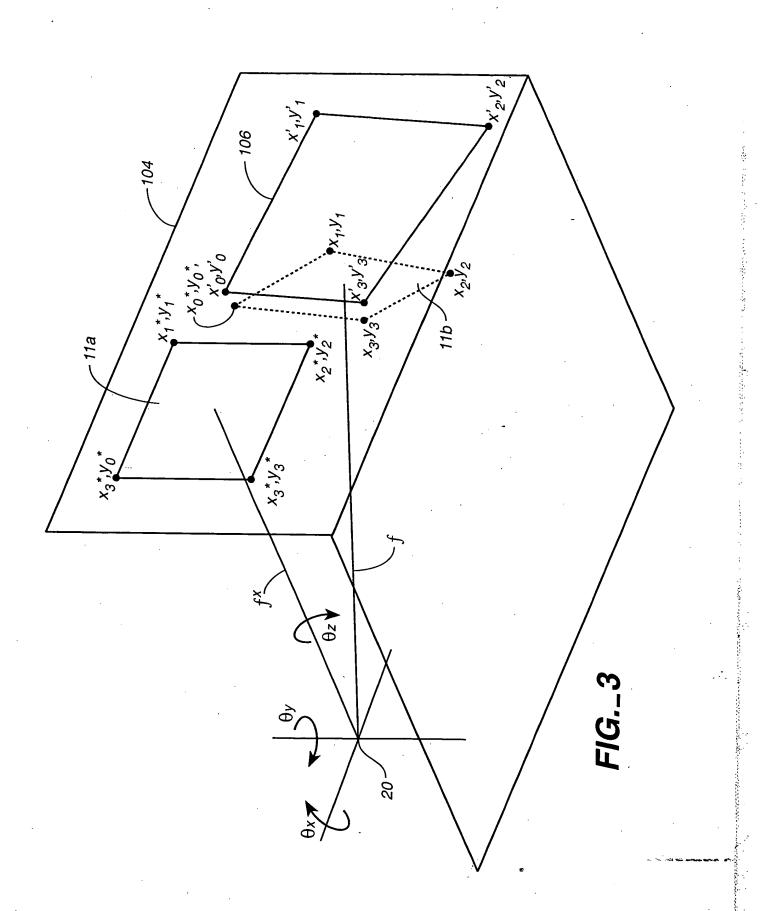
FIG._1







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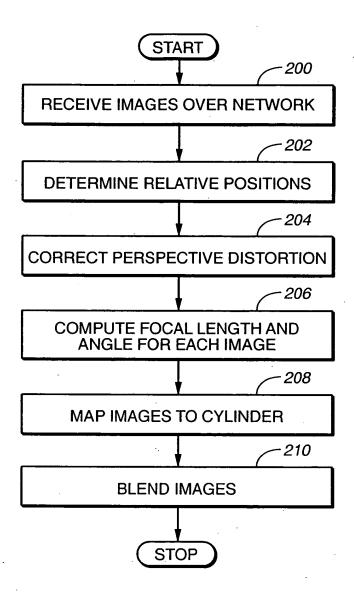
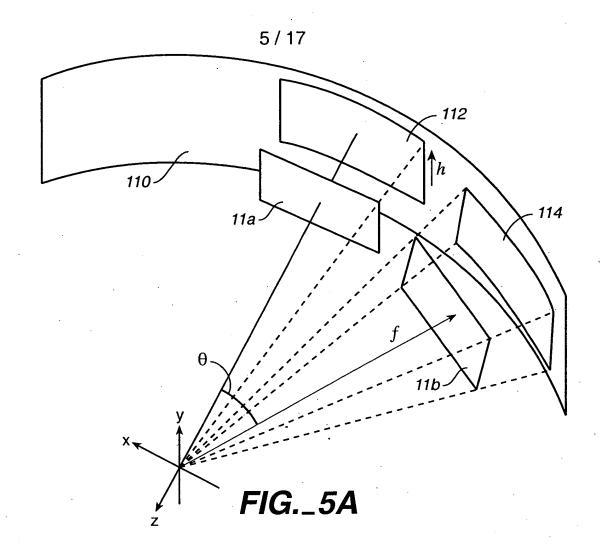
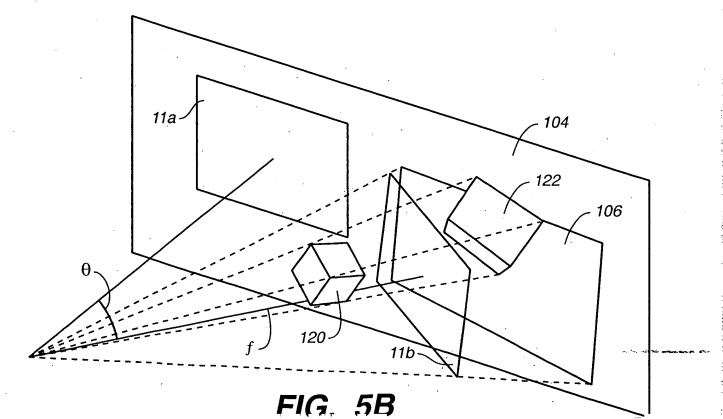
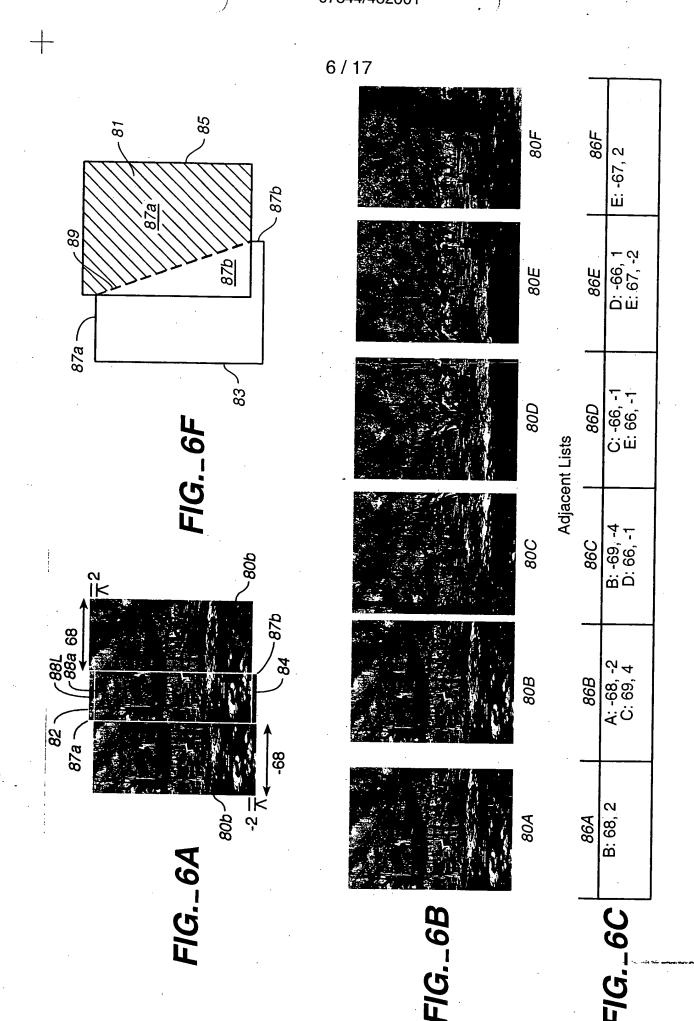
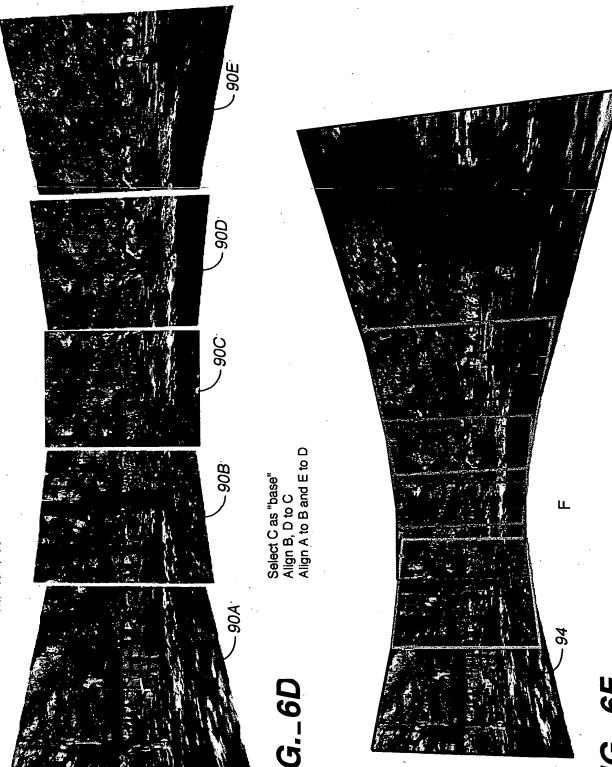


FIG._4

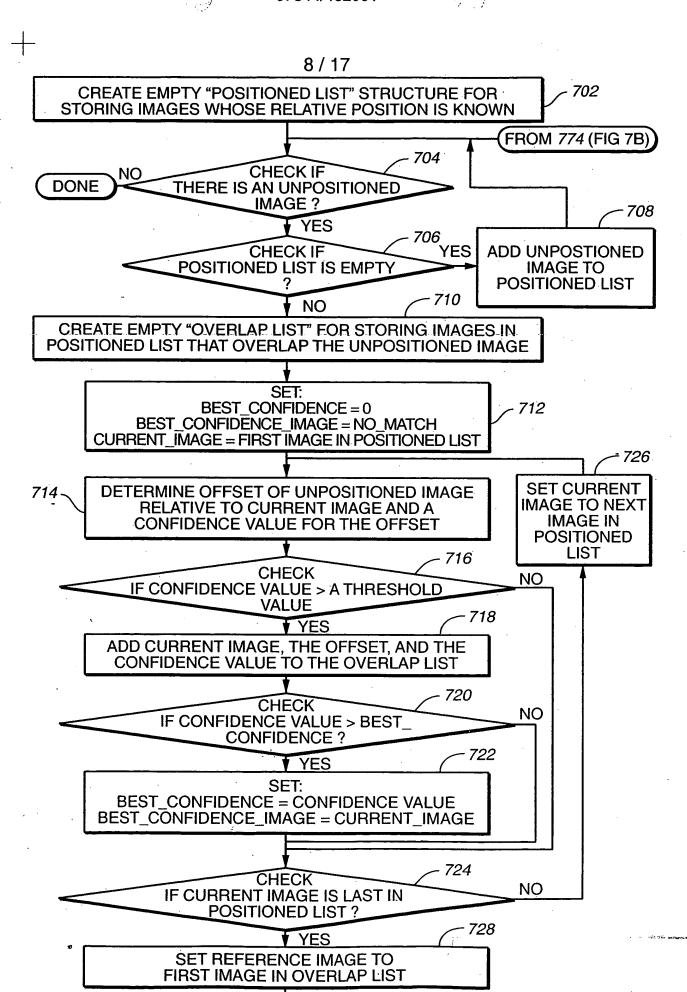


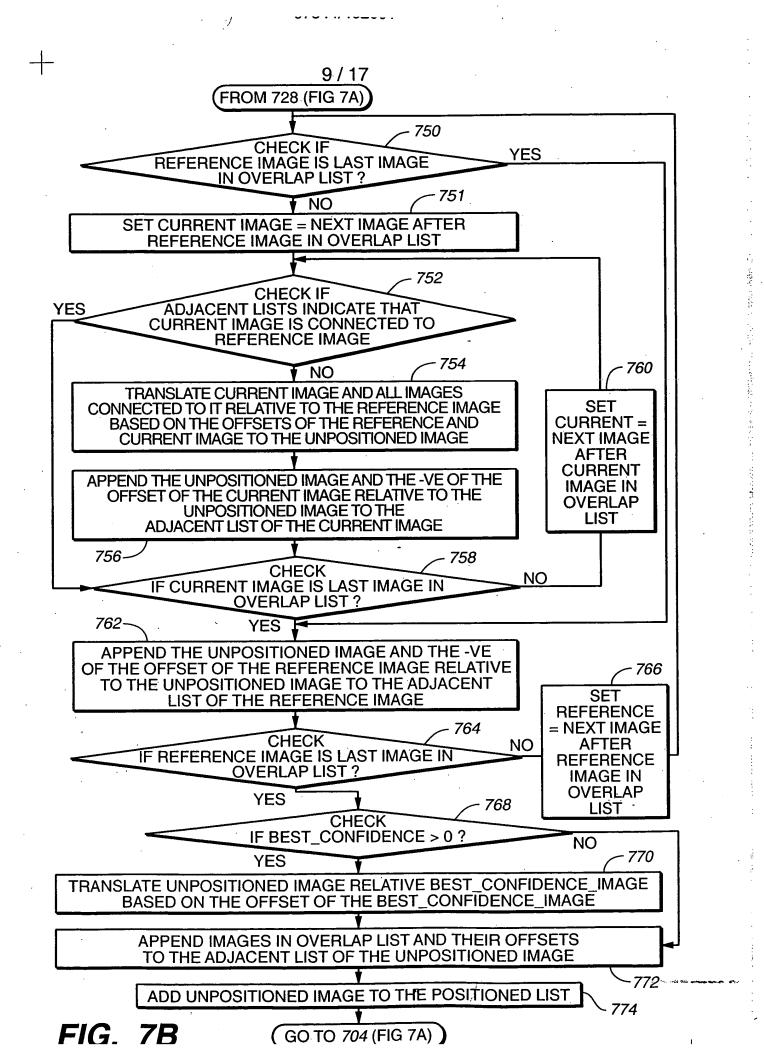


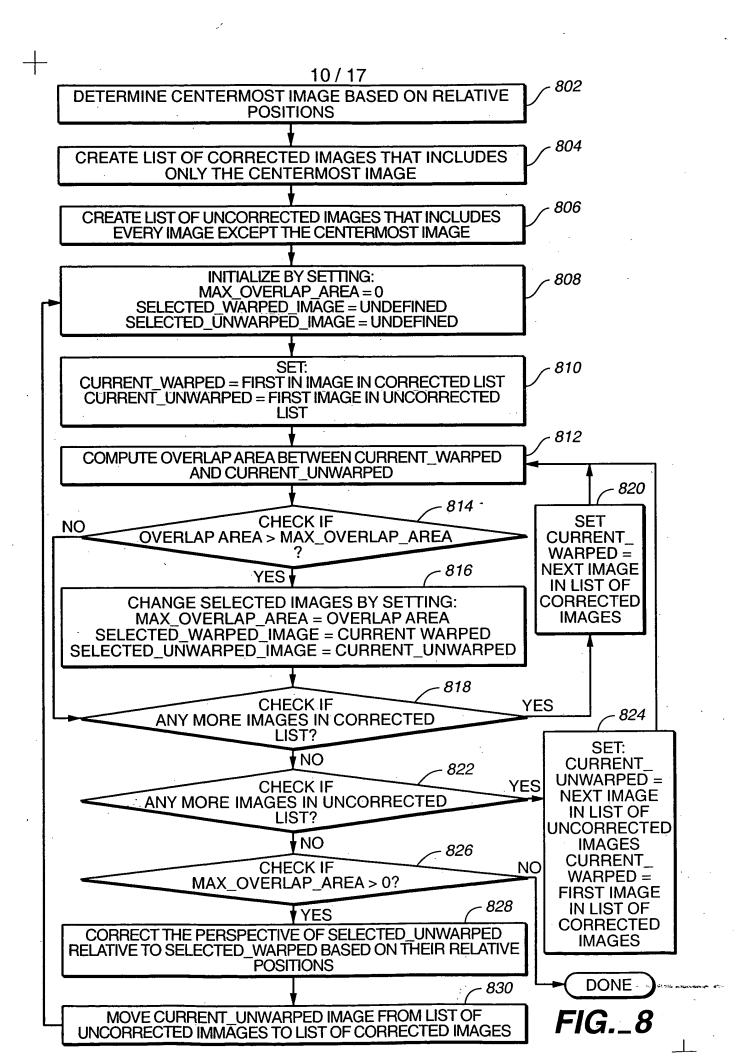




:1G._6E







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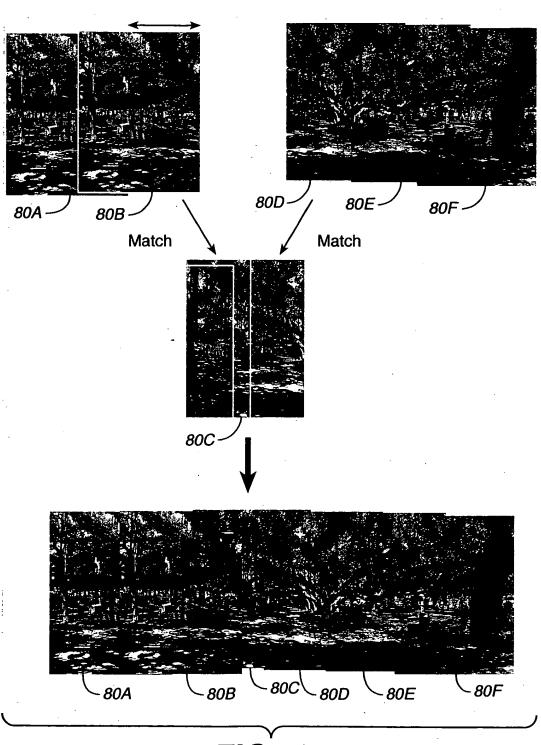


FIG._9

Original Image

	2-D coordinates	4-D coordinates
Vertex 0 Vertex 1 Vertex 2 Vertex 3 The i th vertex	(x_0, y_0) (x_1, y_1) (x_2, y_2) (x_3, y_3) (x_i, y_i)	$ \begin{pmatrix} (x_0, y_0, 0, 1) \\ (x_1, y_1, 0, 1) \\ (x_2, y_2, 0, 1) \\ (x_3, y_3, 0, 1) \\ (x_i, y_i, 0, 1) \end{pmatrix} $ 134

FIG._ 10A

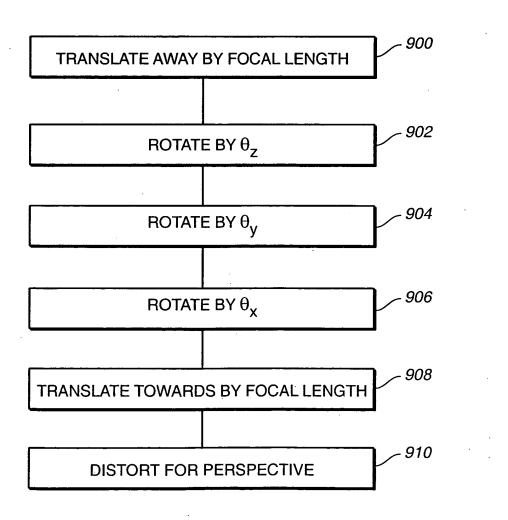


FIG._10B

Perspective Correction Transformation

1. Translate outwards:

$$T_a = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & f & 1 \end{bmatrix}$$
 136

2. Three rotations:

$$\Theta_{x} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos\theta_{x} & \sin\theta_{x} & 0 \\ 0 & -\sin\theta_{x} & \cos\theta_{x} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad \Theta_{y} = \begin{bmatrix} \cos\theta_{y} & 0 & -\sin\theta_{y} & 0 \\ 0 & 1 & 0 & 0 \\ \sin\theta_{y} & 0 & \cos\theta_{y} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\Theta_{z} = \begin{bmatrix} \cos\theta_{z} & \sin\theta_{z} & 0 & 0\\ -\sin\theta_{z} & \cos\theta_{z} & 0 & 0\\ 0 & 0 & 1 & 0\\ 0 & 0 & 0 & 1 \end{bmatrix}$$
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3. Translate inwards:

$$T_b = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & -f & 1 \end{bmatrix}$$

4. Effect of focal length on Perspective:

$$P = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1/f \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

FIG._10C

Perspective Correction

Perspective Corrected Image Vertices given by:

$$\widehat{p}_i = p_i T_a \Theta_z \Theta_y \Theta_x T_b P = \underbrace{\left[\widehat{\mathbf{x}}_i, \widehat{\mathbf{y}}_i, \widehat{\mathbf{z}}_i, \widehat{\mathbf{w}}_i\right]}_{152}$$

But: $\widehat{\mathbf{w}}_i = -\frac{\mathbf{x}_i}{f} \left(-\sin\theta_z \sin\theta_x + \cos\theta_z \sin\theta_y \cos\theta_y \right) \\ + \frac{\mathbf{y}_i}{f} \left(\cos\theta_z \sin\theta_x + \sin\theta_z \sin\theta_y \cos\theta_x \right) \\ + \cos\theta_y \cos\theta_x$

and x_i and y_i from the perspective corrected image are given by:

$$x_i' = \widehat{X}_i / \widehat{W}_i$$
 and $y_i' = \widehat{Y}_i / \widehat{W}_i$
154.

Therefore we can write:

$$F_{xi}(\theta_z, \theta_y, \theta_x, f) - x'_i = 0^{-158}$$

Taking:

$$t = [\theta_x \ \theta_y \ \theta_z \ f] / 160$$

We can write:

$$-\mathbf{F(t)} = \begin{bmatrix} \mathbf{x}_o - F_{x_o}(\mathbf{\theta}_z, \mathbf{\theta}_y, \mathbf{\theta}_x, f) \\ \mathbf{y}_o - F_{y_o}(\mathbf{\theta}_z, \mathbf{\theta}_y, \mathbf{\theta}_x, f) \\ \\ \mathbf{x}_i - F_{x_i}(\mathbf{\theta}_z, \mathbf{\theta}_y, \mathbf{\theta}_x, f) \\ \\ \mathbf{y}_i - F_{y_i}(\mathbf{\theta}_z, \mathbf{\theta}_y, \mathbf{\theta}_x, f) \end{bmatrix}$$
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Newton's Method

By Newton's method of numerical computation, t is an estimate of the values

$$[\theta_x \ \theta_y \ \theta_z \ f]$$

then:

$$t_{new} = t - J^{-l}F(t)$$
 166

is a better estimate of the values.

Where J^{-1} is the matrix of partial derivatives:

$$J_{i,j} = \frac{\partial F_i}{\partial t_j} 164$$

FIG._10E

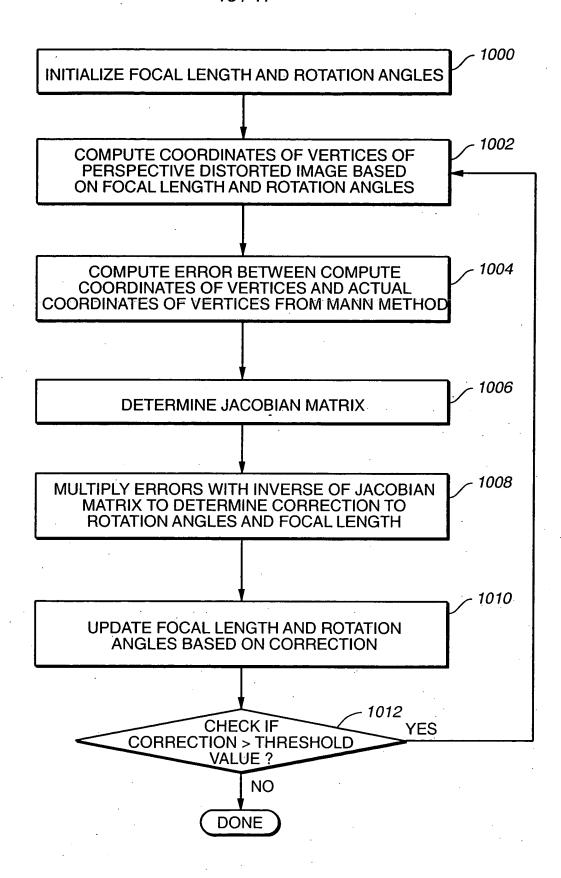


FIG._11

